UNIVERSITY OF CAMBRIDGE INTERNATIONAL EXAMINATIONS GCE Ordinary Level

MARK SCHEME for the May/June 2012 question paper for the guidance of teachers

4024 MATHEMATICS (SYLLABUS D)

4024/22 Paper 2, maximum raw mark 100

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Abbreviations

cao correct answer only cso correct solution only

dep dependent

ft follow through after error isw ignore subsequent working

oe or equivalent SC Special Case

www without wrong working

soi seen or implied

SECTION A

| Qu | | Answers | Mark | Part marks |
|----|---------|--|-----------|---|
| 1 | (a) | pentagon | 1 | |
| | (b) | $x \le 5$ oe $x + y \le 6$ oe | 1 1 | After $0 + 0$, C1 for $x \dots 5$ oe and $x + y \dots 6$ oe with incorrect (in)equalities for "". |
| | (c) | line passing through (5, 0) and (8, 3) | 1 | |
| | (d) | -1 cao | 1 | |
| 2 | (a) | $x = \frac{3}{5}$ oe | 2 | M1 for $14x + 2 - 4x - 8$ (= 0) or better |
| | (b) | $y = \pm 9$ | 1 | |
| | (c) (i) | h(h+6) = 33.25 | M1 | |
| | | Rearranging correctly to give $4h^2 + 24h - 133 = 0$ | A1 | |
| | (ii) | h = 3.5 oe and -9.5 oe | 3 | Using $\frac{p \pm (or + or -)\sqrt{q}}{r}$ |
| | | | | B1 for $p = -24$ and $r = 8$ (or 2×4) B1 for $q = 24^2 - 4 \times 4 \times (-133)$, or 2704 |
| | | | | or $\sqrt{q} = 52$ |
| | | | | Using factors B2 for $(2h-7)(2h+19)$ (= 0) |
| | | | | or B1 for $(2h 7)(2h 19)$ (= 0) |
| | | | | where are not both the correct signs |
| | (iii) | 9.5 cm or <i>their</i> (positive h) + 6 | 1 ft | |

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| 3 | (a) | 36 minutes cao | 1 | |
|---------|---------|---|-------------|---|
| | (b) | 5 km/h cao | 1 | |
| | (c) | \$5.2(0) | 2 | M1 for $85\% = 4.42$ oe |
| | (d) | Horizontal line from (1800, 4) to (2000, 4) | 1 | |
| | | Line from (2000, 4) to (2030, 2.5) or ft from (their 2000, 4) to ((their 2000) + 30, 2.5) | 1 ft | |
| | (e) | 20 30 or (their 2000) + 30 | 1 ft | |
| 4 | (a) | 279° to 283° | 1 | |
| | (b) | Y correctly positioned with two correct construction arcs | 2 | M1 for correctly positioned Y with one correct construction arc, or with no construction arcs or M1 for Y above WX and two correct construction arcs |
| | (c) | Z on a bearing of 072° from W Z is due North of X 27 to 29 km | 1 1 1 | |
| 5 | (a) (i) | 25, 9 | 1 | |
| | (ii) | 7.15 to 7.25 | 1 | |
| | (iii) | 1.1 to 1.3 | 2 | M1 for 7.75 to 7.85 and 6.55 to 6.65 seen |
| | (iv) | $\frac{22}{60}$ oe, or 0.36 to 0.37, or 36 to 37% | 2 | B1 for 22 seen or C1 for $\frac{38}{60}$ oe |
| | (b) (i) | 5.65 cm | 3 | M1 for $3.5 \times 4 + 4.5 \times 15 + 5.5 \times 20 + 6.5 \times 13 + 7.5 \times 5 + 8.5 \times 3$ i.e. $14 + 67.5 + 110 + 84.5 + 37.5 + 25.5$ (= 339) M1 for \div 60 (or $4 + \dots$) |
| | (ii) | 35% | 2 | B1 for 65%, or for 21 seen |
| 6 | (a) (i) | 4, 8, 10, 14 | 1 | |
| | (ii) | 1 | 1 | |
| | (iii) | 3 out of {2, 5, 7, 11, 13} | 1 | |
| | (b) | Correct shading | 1 | |
| | (c) | 16 | 2 | B1 for Venn Diagram and 17 in $(G \cup S)'$ |
| <u></u> | | | | |

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| 7 (a) (i) | b – a | 1 | |
|-----------|--|------|---|
| (ii) | $\frac{1}{2}(\mathbf{b}+\mathbf{c})$ | 1 | |
| (iii) | $\frac{1}{4}\mathbf{b} + \frac{1}{2}\mathbf{c} \text{or their (aii)} - \frac{1}{4}\mathbf{b}$ | 2 ft | B1 for one correct term or for $-\frac{1}{4}\mathbf{b} - \frac{1}{2}\mathbf{c}$ |
| (b) (i) | $\frac{2}{5}\mathbf{b} - \frac{2}{5}\mathbf{a}$ | 1 | |
| . , | 2:3 oe | 1 | |
| (iii) | $\frac{3}{5}\mathbf{a} - \frac{7}{20}\mathbf{b} - \mathbf{c}$ | 2 | B1 for one correct term, or for $\mathbf{c} + \frac{7}{20}\mathbf{b} - \frac{3}{5}\mathbf{a}$ |

SECTION B

| 8 (a) (i) | 128 to 128.4 | 3 | M2 for $\cos B = \frac{20^2 + 2^2 - 21.3^2}{2 \times 20 \times 2}$ |
|-----------|--------------|---|--|
| | | | or M1 for $21.3^2 = 20^2 + 2^2 - 2 \times 20 \times 2 \times \cos B$ |
| (ii) | 14.3 to 14.5 | 3 | M2 for sin $((their(ai) - 90) = \frac{x}{20}$ oe (12.4) |
| (b) (i) | 29° | 1 | |
| (ii) | 9.6 to 9.7 | 3 | M2 for $CE = \frac{8.6 \times \sin 33}{\sin(their(bi))}$ |
| | | | or M1 for $\frac{CE}{\sin 33} = \frac{8.6}{\sin(their(bi))}$ oe |
| (iii) | 11.6 to 11.7 | 2 | C1 for 78.3 to 78.4 or B1 for 11.6 to 11.7 or 78.3 to 78.4 seen in working |

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| 9 | (a) (i) | $ \begin{pmatrix} -5 & 0 \\ 1 & 2 \end{pmatrix} $ | 1 | |
|----|-----------|--|----------------|---|
| | (ii) | $\begin{pmatrix} 0 & -\frac{1}{3} \\ \frac{1}{2} & \frac{1}{6} \end{pmatrix} \text{ or } \frac{1}{6} \begin{pmatrix} 0 & -2 \\ 3 & 1 \end{pmatrix} \text{ seen}$ | 2 | M1 for $\begin{pmatrix} 0 & -2 \\ 3 & 1 \end{pmatrix}$ seen, or for attempting to multiply $\frac{1}{6}$ by a 2×2 matrix |
| | (b) (i) | (974) (328) | 2 | B1 for one correct value, or for (974 328) |
| | (ii) | Mention of cost and (both carpet and underlay) | 1 | |
| | (c) (i) | F correctly positioned | 2 | M1 for 2 correct vertices plotted or C1 for correct reflection in $y = x$ |
| | (ii) | G correctly positioned | 2 | M1 for 2 correct vertices plotted or for 3 correct coordinates calculated |
| | (iii) (a) | 4; or –4 | 1 | |
| | (iii) (b) | m = 1, $n = their(c)(iii)(a)$ | 1 ft strict | |
| 10 | (a) (i) | 686 to 687 cm ² | 4 | M1 for using $\frac{300}{360}$ oe M1 for using $\pi \times 15^2$ M1 for $\frac{1}{2} \times 15^2 \times \sin 60$ oe (= 97.4278) |
| | (ii) | 93.5 to 93.6 cm | 2 | M1 for $\frac{300}{360} \times 2 \times \pi \times 15$ (= 78.5398) |
| | (b) | 12.4 cao | 2 | B1 for $\frac{1}{2}(15+25)h = 248$ oe |
| | (c) (i) | 3 | 1 | |
| | (ii) | 37.36 to 37.4 cm ² | 3 | M1 for 248 + their(a)(i) M1 for division by 5 ² soi (indep) |

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| 11 (a) (i) | 56° | 1 | |
|-------------|---|------|--|
| (ii) | $34^{\circ} \text{ or } 90 - their(a)(i)$ | 1 ft | |
| | | | |
| (iii) | 62° or $(180 - their(a)(i))/2$ | 1 ft | |
| (iv) | 42° | 2 | B1 for $\hat{ACD} = 28^{\circ}$ seen |
| (v) | 110° | 2 | B1 for seeing $D\hat{A}C = 42^{\circ}$; or $A\hat{B}C = 70^{\circ}$; or $A\hat{B}O = 8^{\circ}$ |
| (b) (i) (a) | 32° alternate (to $P\hat{Q}T$) | 1 | If $0 + 0$, then C1 for both 32° and 116° |
| (i) (b) | 116° \hat{SPQ} and \hat{PQR} are allied, interior, adjacent | 1 | |
| (ii) | Full line parallel to <i>PS</i> , 4 cm away Full arc, centre <i>R</i> , radius 5 cm | 1 1 | |
| (iii) | Correct region shaded | 1 ft | |
| 12 (a) | Convincing reason. e.g. The height of the cuboid would then be –2 cm | 1 | |
| (b) | $x^{2}(8-x) \text{ and } \frac{4}{3} \times 3 \times (\frac{x}{2})^{3}$ | M1 | |
| | Correct expansion and simplification to $8x^2 - \frac{x^3}{2}$ | A1 | |
| (c) (i) | 58.5 | 1 | |
| (ii) | 7 correct plots and a smooth curve | 3 | B2 for 6 or 7 correct (ft) plots or B1 for 4 or 5 correct (ft) plots |
| (iii) | 3.3 to 3.5 | 2 | B1 for 4.5 to 4.7 seen |
| (d) | $4.7 \le x < 5 \text{ (dep on M1)}$ | 3 | B1 for $(y =) 27x$ seen or implied M1 for attempt at drawing correct line |